

Velocity/multi-scalar measurements in turbulent co-axial jets

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Background and Motivation

- Scalar mixing in turbulent flows plays an important role in many applications, both industrial and environmental:
 - Heat transfer, combustion, environmental pollution dispersion, atmospheric & oceanic sciences
- However, most scalar mixing studies have focused on the mixing of a single scalar
 - There has comparatively been relatively little work on multi-scalar mixing



Background and Motivation (cont.)

- Nevertheless, there have been some studies of multi-scalar mixing:

	Experimental	Computational
Homogenous, Isotropic Turbulence	<ul style="list-style-type: none"> Warhaft (1981) Sirivat and Warhaft (1982) Warhaft (1984) 	<ul style="list-style-type: none"> Juneja and Pope (1996) Vrieling and Nieuwstadt (2003) Viswanathan and Pope (2008)
Jets	<ul style="list-style-type: none"> Tong and Warhaft (1995) Cai et al. (2011) Soltys and Crimaldi (2015) Li et al. (2017) 	<ul style="list-style-type: none"> Rowinski and Pope (2013)
Channel Flow	<ul style="list-style-type: none"> Costa-Patry and Mydlarski (2008) 	<ul style="list-style-type: none"> Oskouie et al. (2015)
Boundary Layers	<ul style="list-style-type: none"> Sawford et al. (1985) Davies et al. (2000) 	
Mixing Layers		<ul style="list-style-type: none"> Cha et al. (2006) Sawford (2006) Sawford and de Bruyn Kops (2008) Meyer and Deb (2012)

Objectives: short, medium and longer term

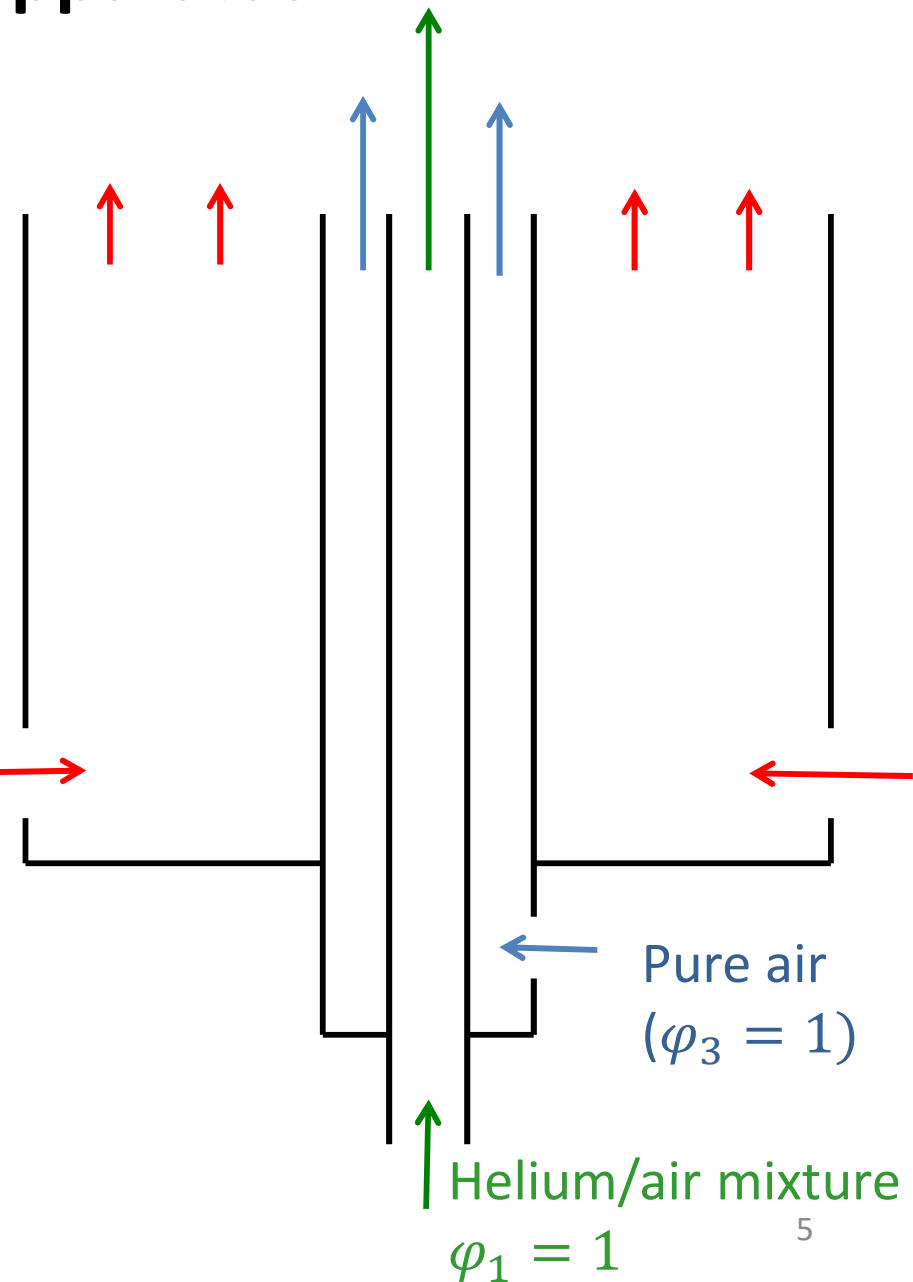
- To develop a measurement technique capable of simultaneously measuring of **two scalars and velocity** in turbulent flows at high temporal and spatial resolution
- To (experimentally) study the evolution of two distinct scalars (temperature and helium) in a turbulent coaxial jet
 - Inspired by the experiment of Cai et al., *J. Fluid Mech.* (2011)
- To provide data for the testing of mixing models with the aim of (hopefully) validating and/or further improving them for use in multi-scalar mixing applications, similar to what has been undertaken by Cai et al., *J. Fluid Mech.* (2011) and Rowinski and Pope, *Phys. Fluids* (2013)

Experimental Apparatus

- Vertically oriented coaxial jet emanating into a co-flow of heated air (based on the experimental set-up of Cai *et al. J. Fluid Mech.*, 2011)
 - 1st (central) jet:
 - fully developed flow
 - mixture of helium (4% by mass) and air (96% by mass)
 - 2nd (annular) jet:
 - fully developed flow
 - pure (unheated) air
 - 3rd co-flow:
 - approximately uniform flow
 - heated air ($\Delta T = 6.0 \text{ }^\circ\text{C}$)

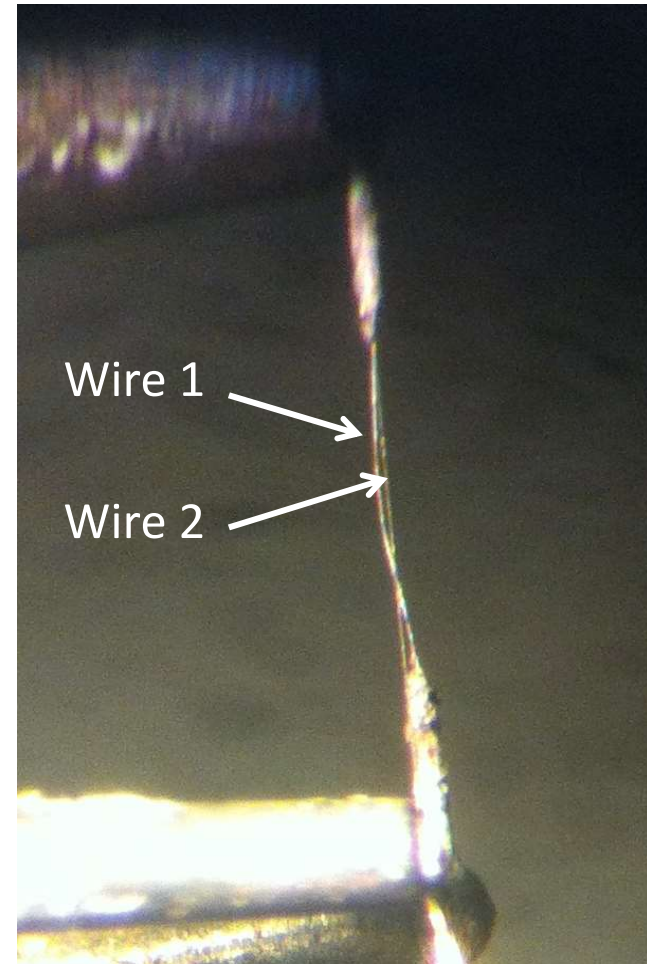
Heated air
 $\varphi_2 = 1$

	1 st jet	2 nd jet	3 rd jet
U at jet exit	12.6 m/s	11.3 m/s	0.4 m/s
Re_{D_h}	3900	2300	3600
D_h	0.622 cm	0.318 cm	13.34 cm



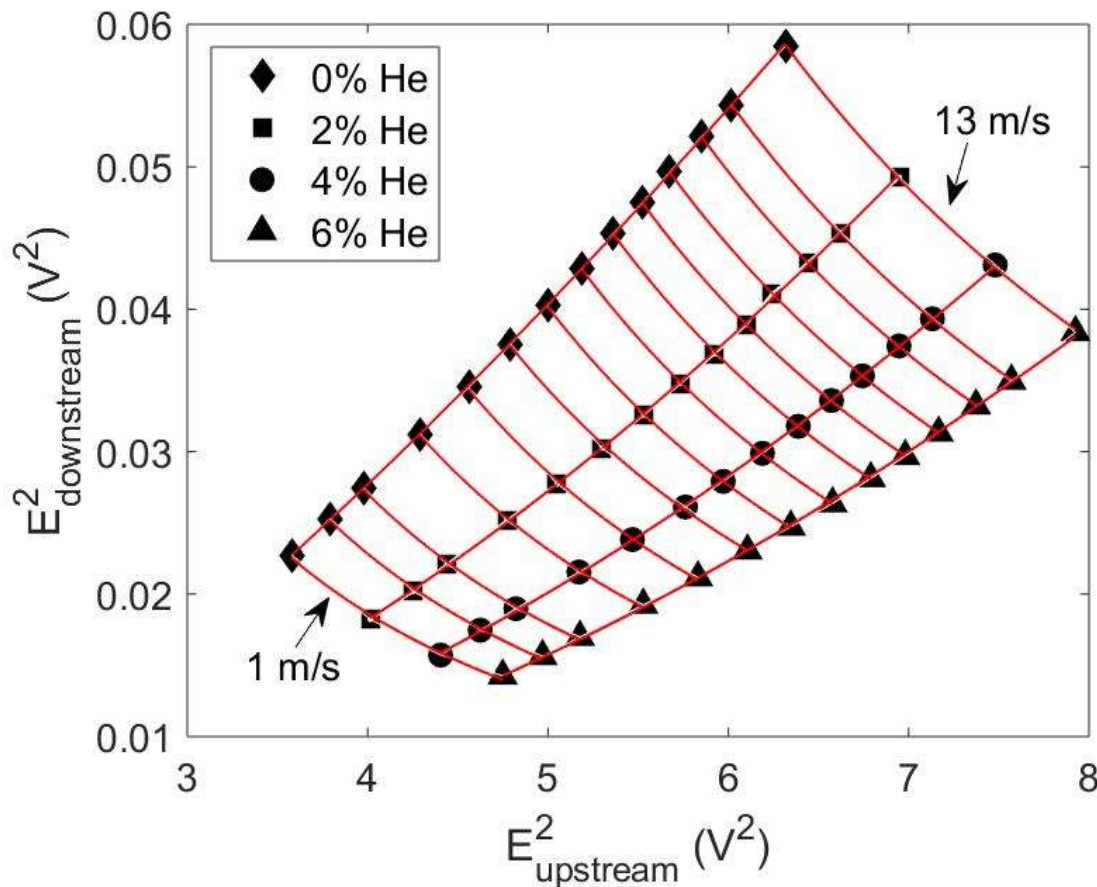
3-Wire Thermal Anemometry Probe for Simultaneous Measurements of U, C and T

- 3-wire probe consists of:
 - **Two** hot-wires to measure the velocity and concentration (“Interference” or “Way-Libby” probe)
 - Wires are placed close together (5-15 μm)
 - **One** cold wire (not shown) to measure the temperature (insensitive to velocity and concentration)



Interference probe to simultaneously measure velocity and concentration₆

Interference Probe for Isothermal Case



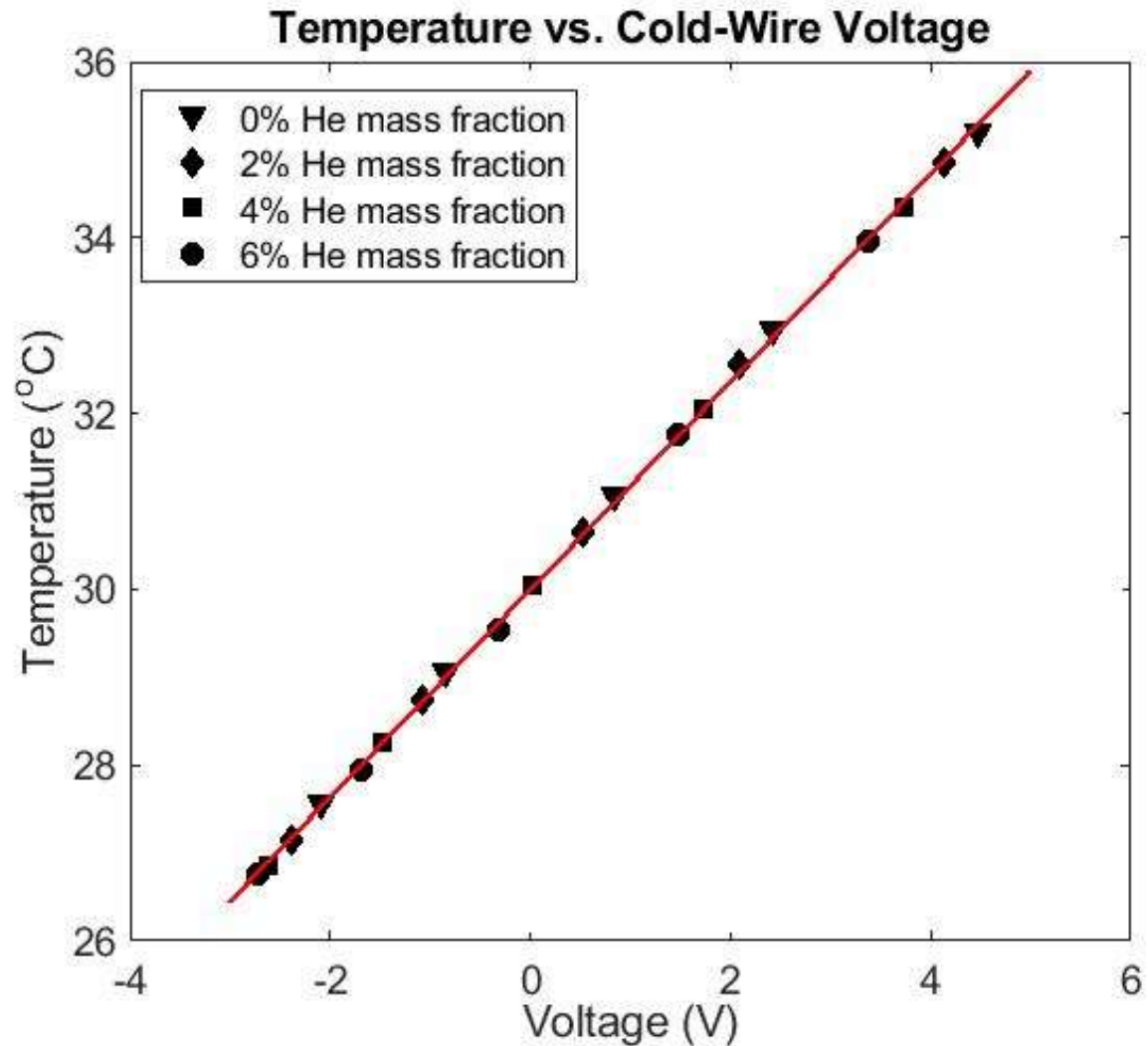
- Concentration determined from a function of both wire voltages:
- $$C = f(E_{up}^2, E_{down}^2)$$
- Upstream wire follows King's Law:

$$U = \left[\frac{E_{up}^2 - A(C)}{B(C)} \right]^{1/n}$$

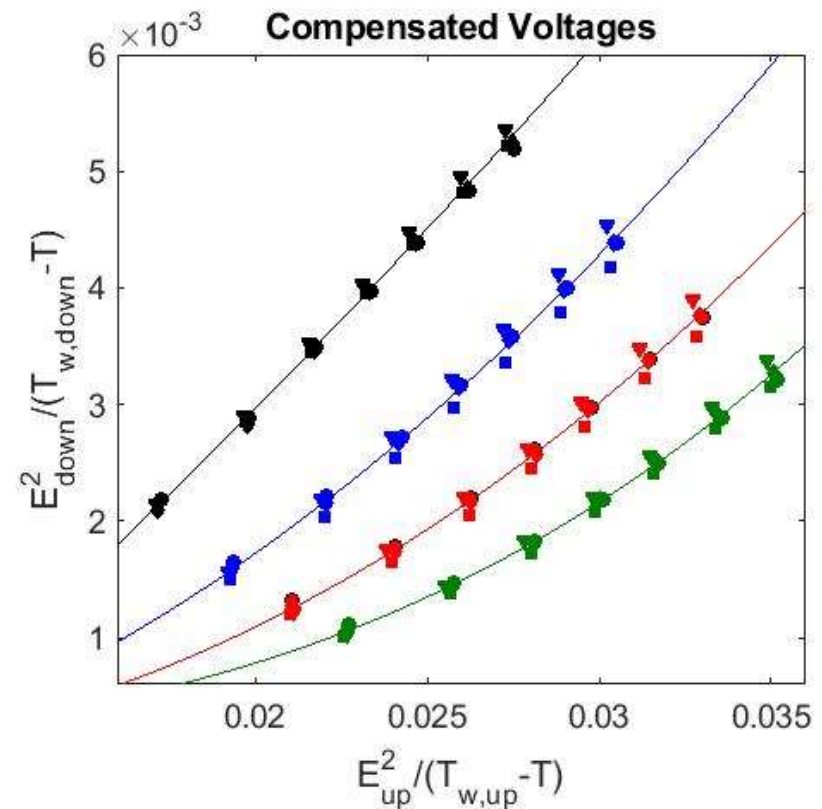
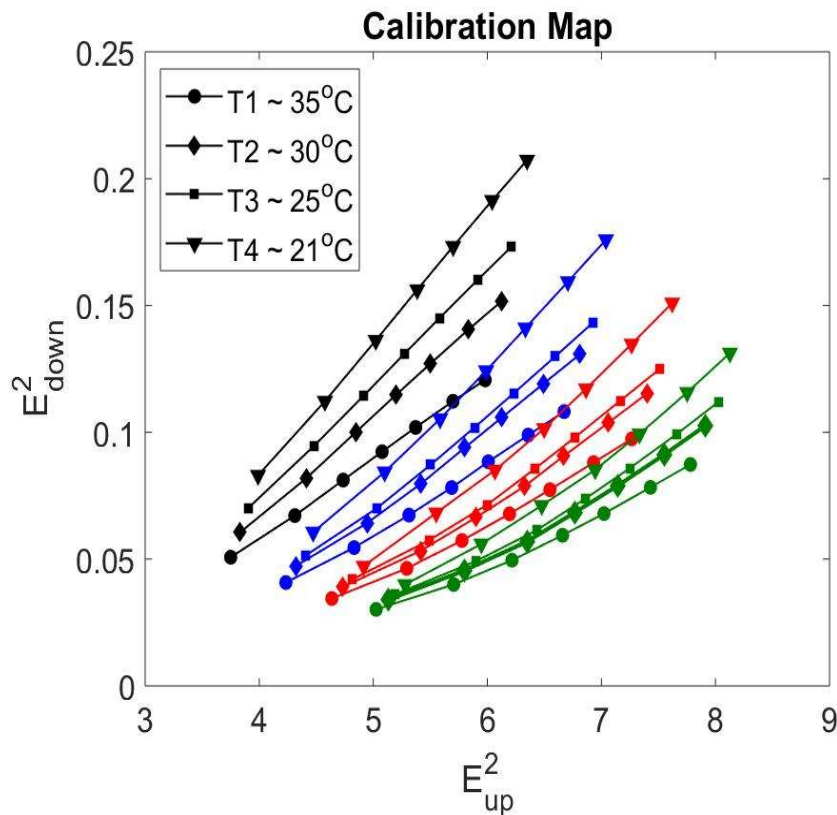
Cold-Wire Thermometer

- Temperature is linearly related to the voltage drop across the sensor:

$$T = A_t + B_t V$$
- Low sensitivity to the fluctuating velocity and He concentration

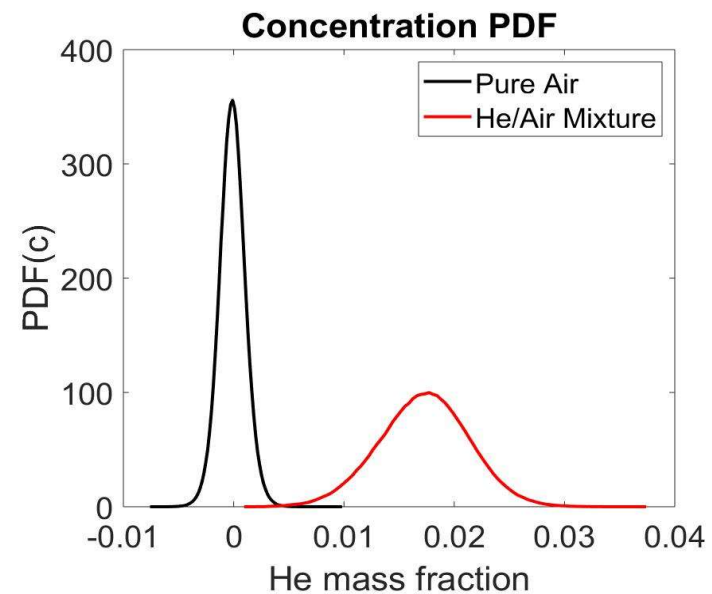
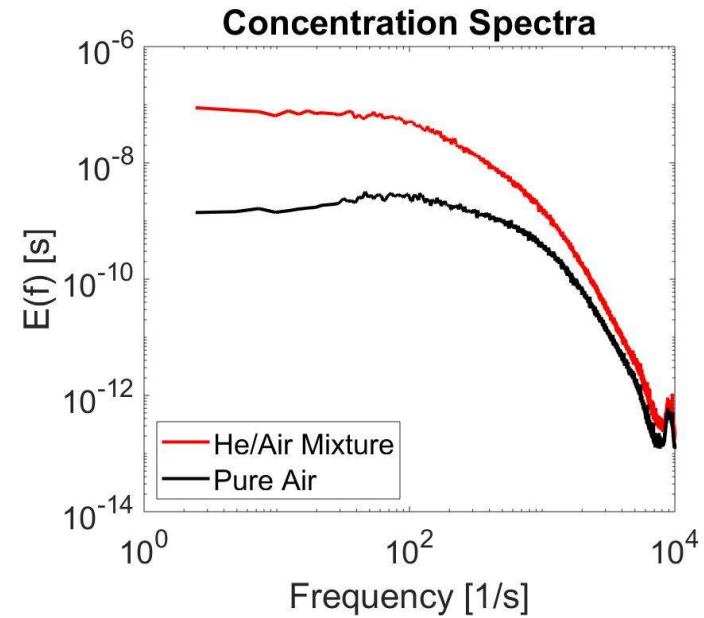
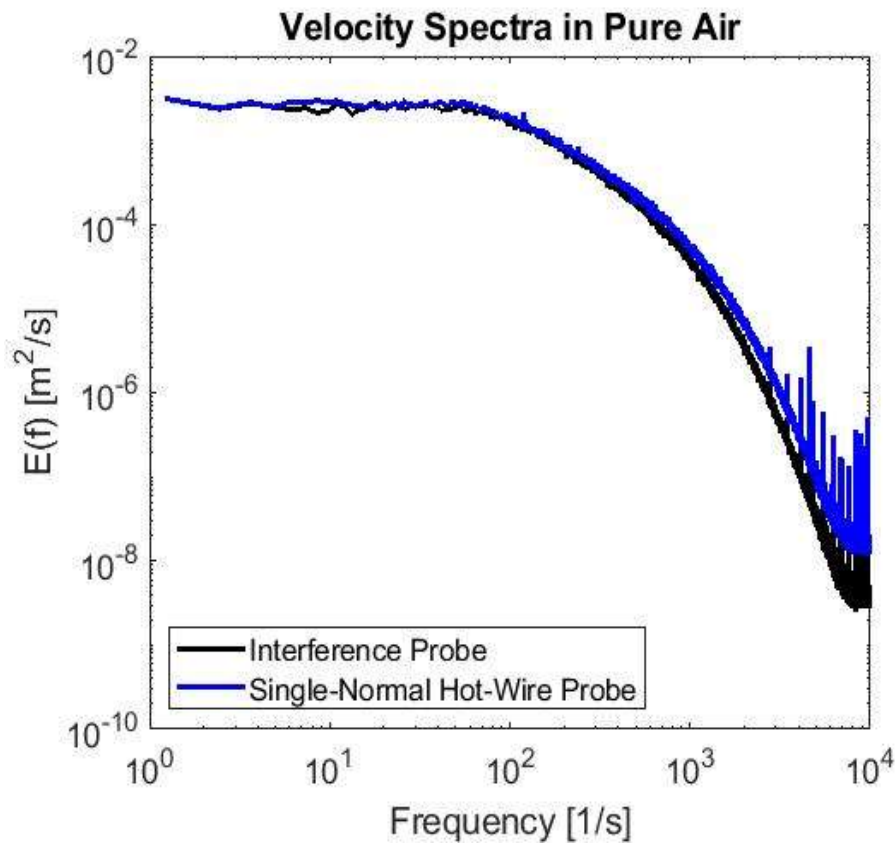


Interference Probe: Extension to **Non-Isothermal Case**

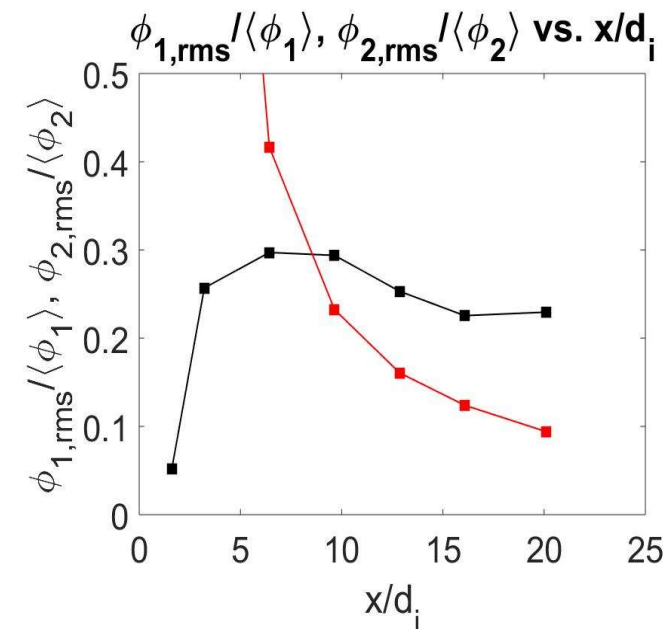
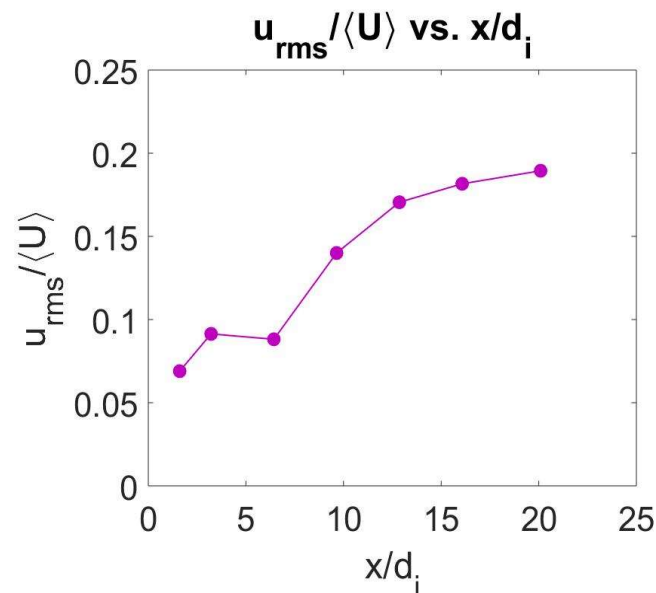
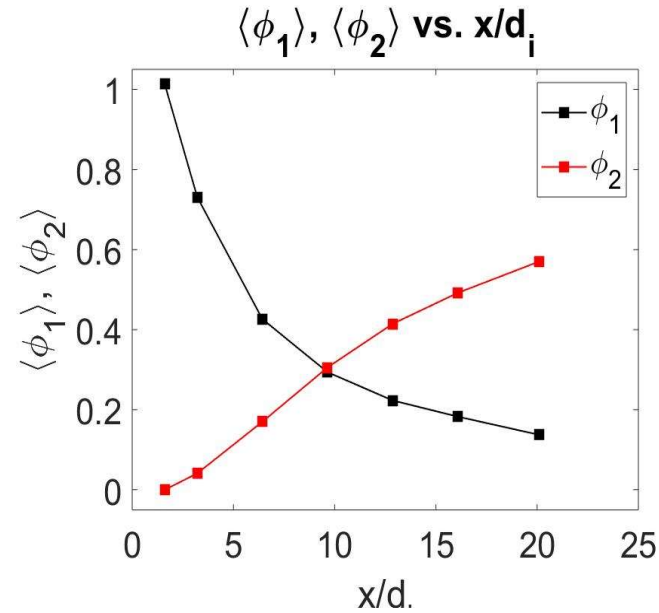
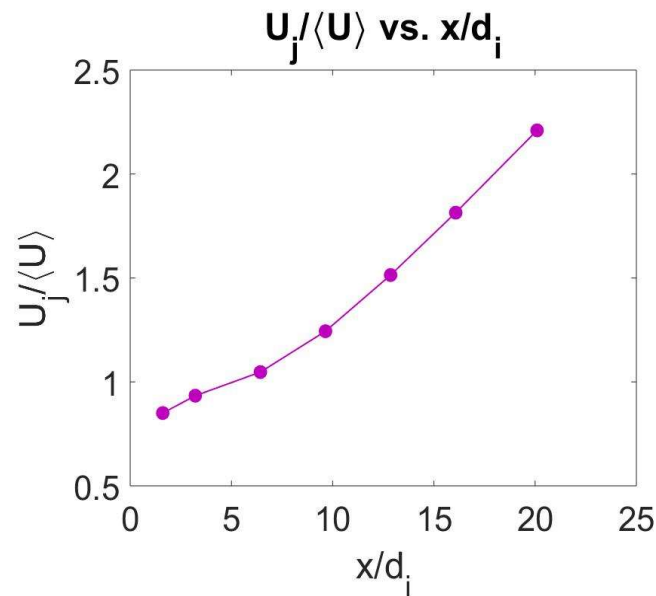


- Black: 0% He mass fraction
- Blue: 2% He mass fraction
- Red: 4% He mass fraction
- Green: 6% He mass fraction

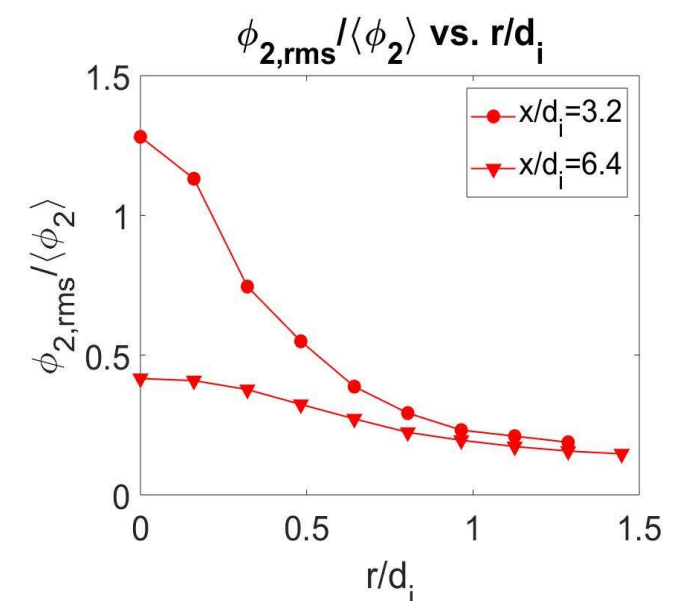
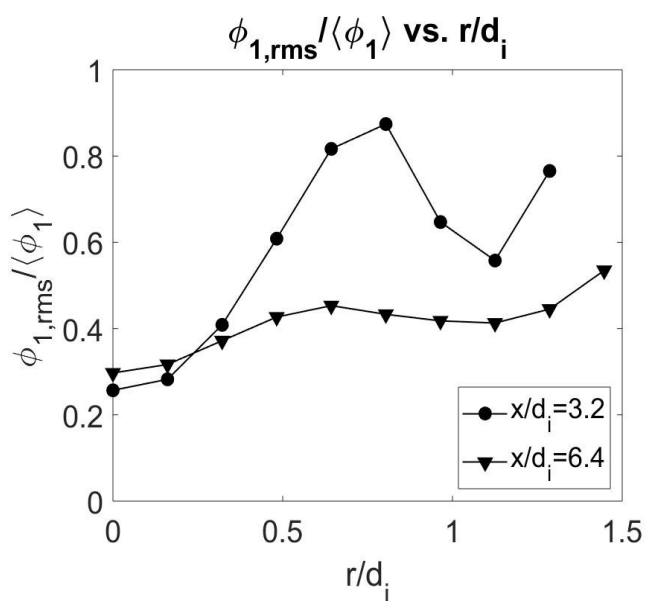
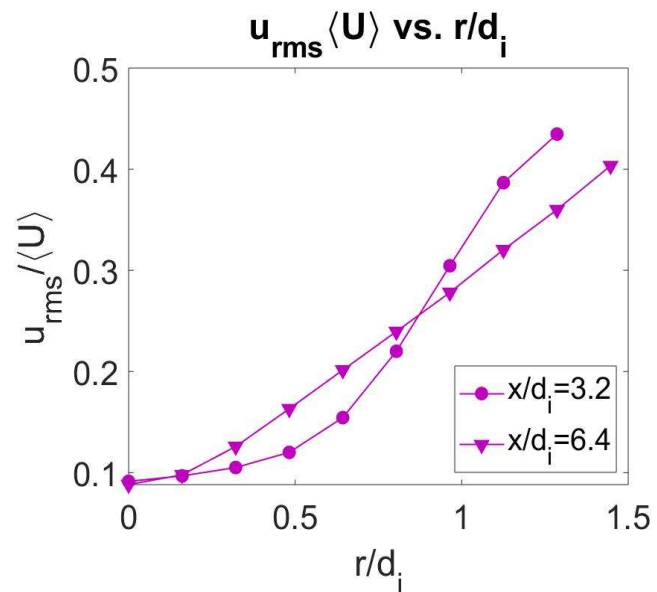
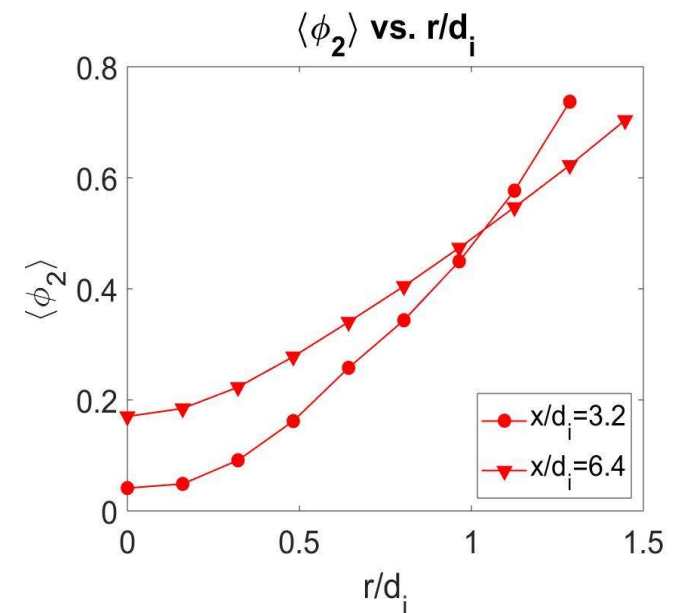
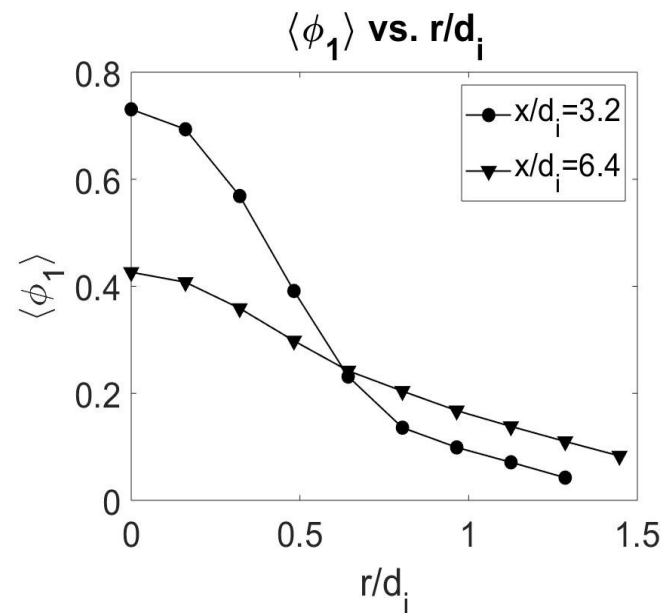
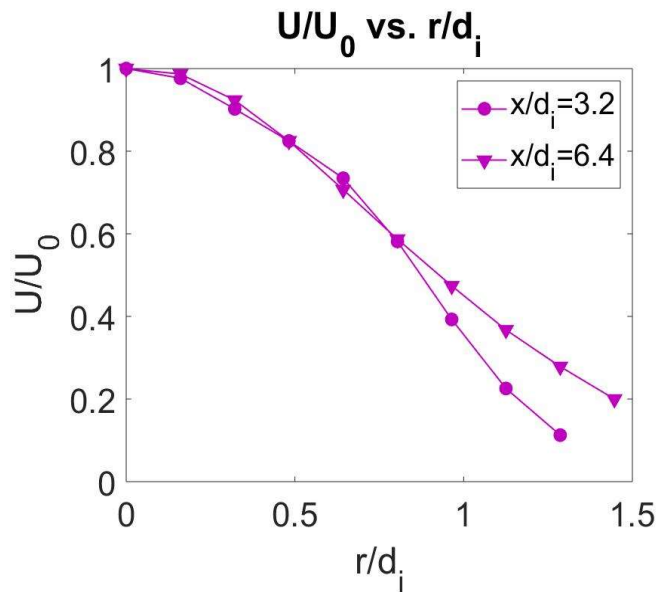
Validation of Interference Probe



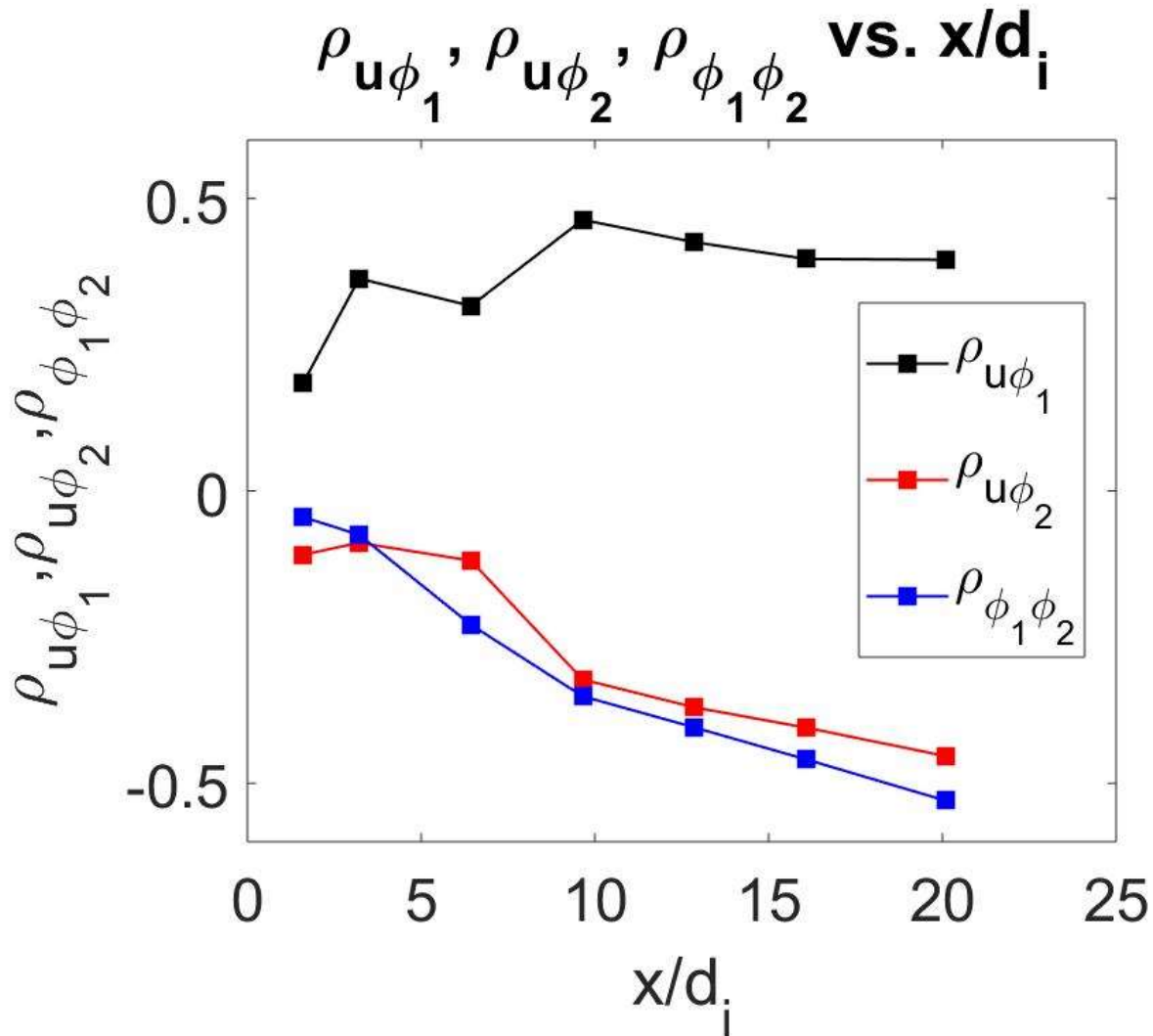
Results: Downstream Evolution of Centerline Statistics



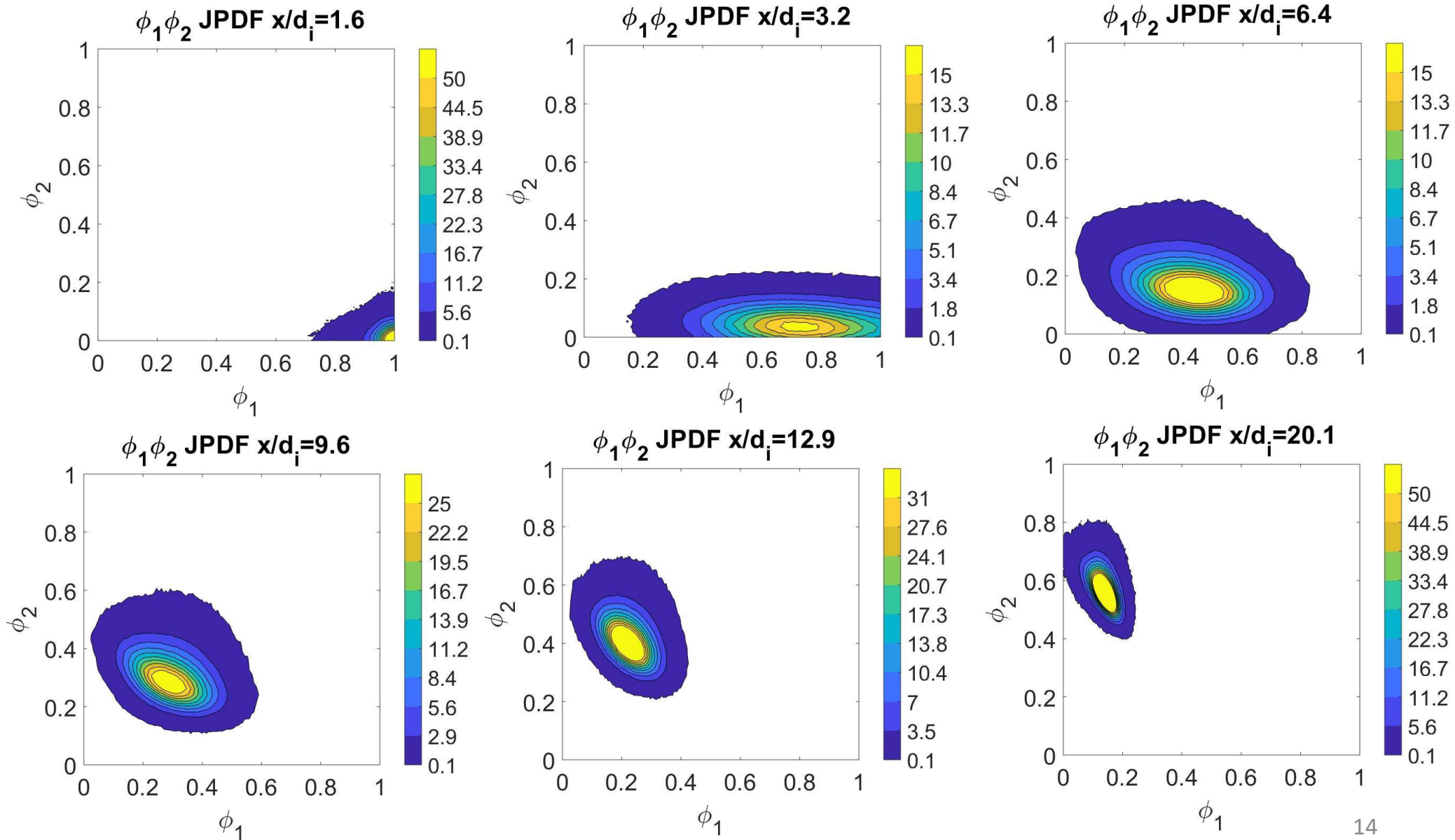
Results: Radial Profiles



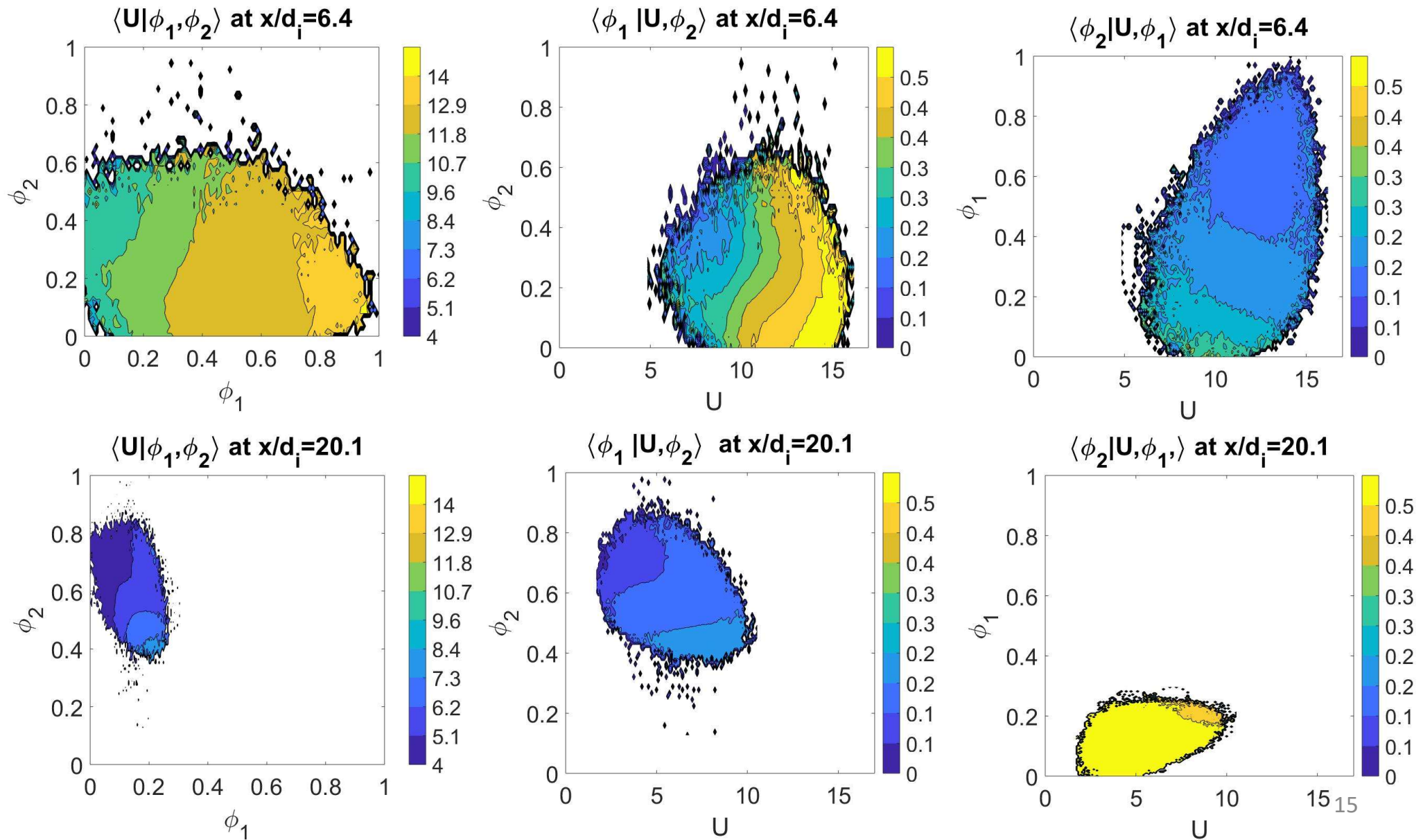
Results: Mixed Statistics → Correlation Coefficients



Results: Downstream Evolution of JPDFs of ϕ_1 and ϕ_2

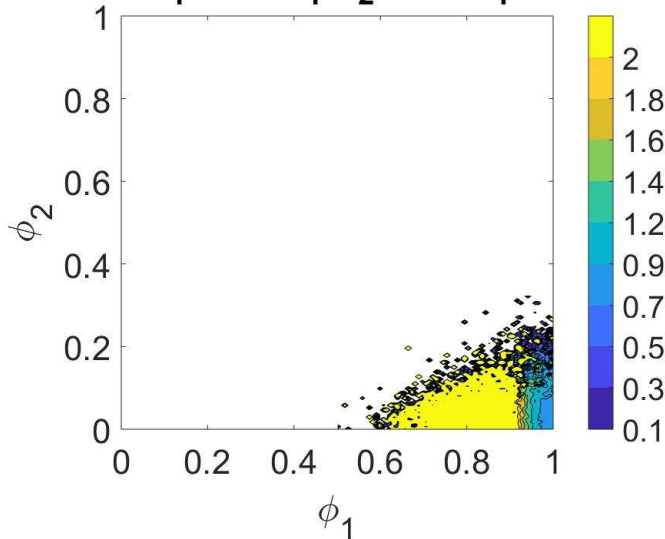


Results: Conditional Expectations

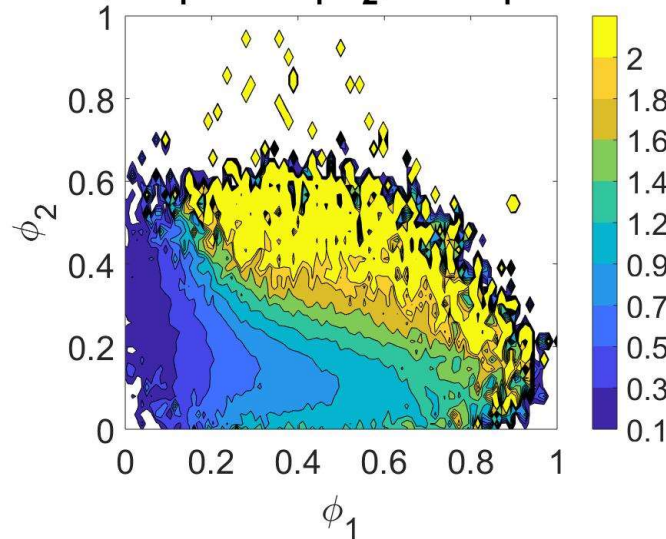


Results: Centerline Conditional Dissipations

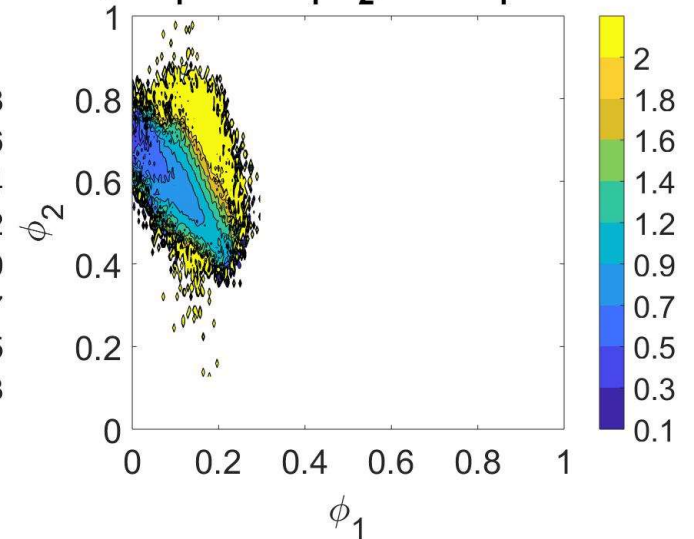
$\langle (\partial\phi_1/\partial x)^2 | \phi_1, \phi_2 \rangle$ at $x/d_i=1.6$



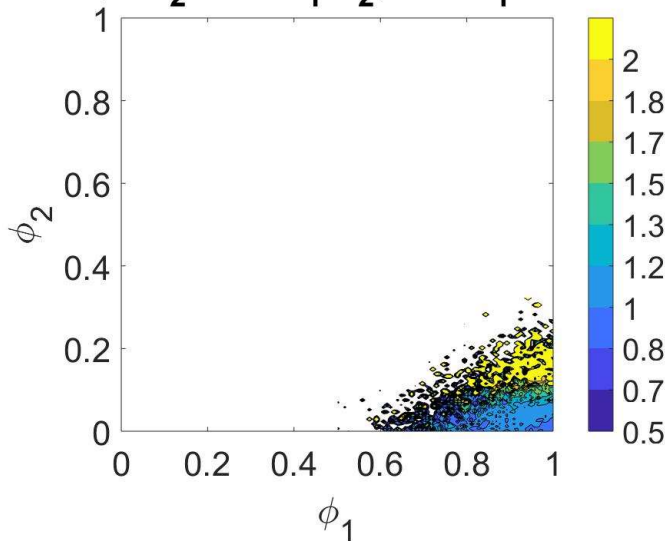
$\langle (\partial\phi_1/\partial x)^2 | \phi_1, \phi_2 \rangle$ at $x/d_i=6.4$



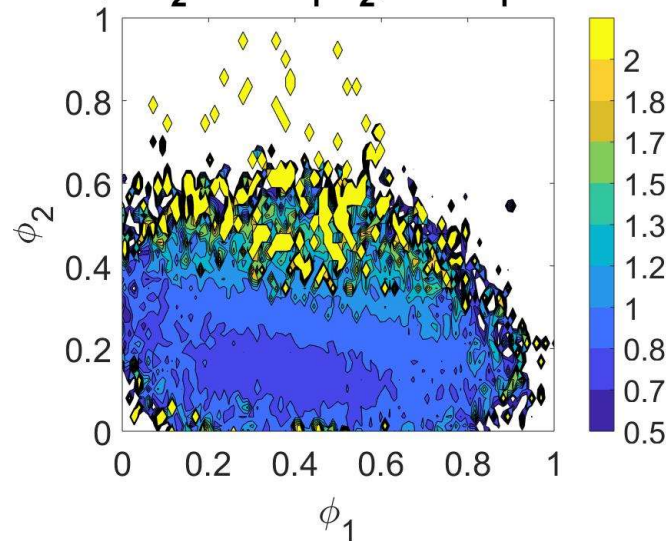
$\langle (\partial\phi_1/\partial x)^2 | \phi_1, \phi_2 \rangle$ at $x/d_i=20.1$



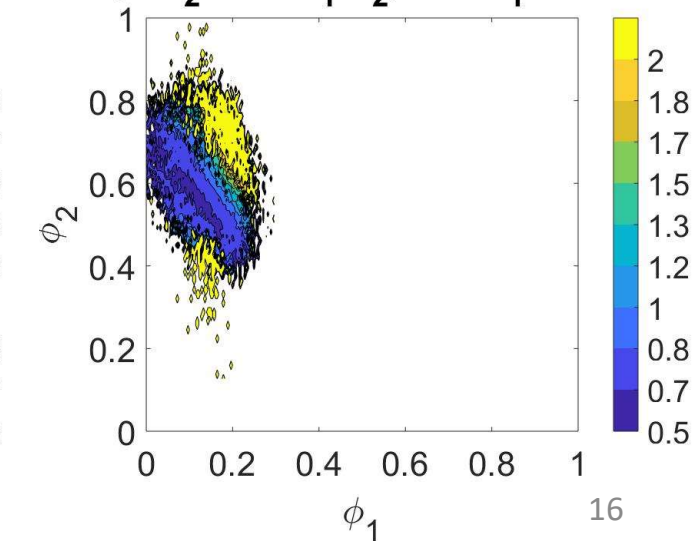
$\langle (\partial\phi_2/\partial x)^2 | \phi_1, \phi_2 \rangle$ at $x/d_i=1.6$



$\langle (\partial\phi_2/\partial x)^2 | \phi_1, \phi_2 \rangle$ at $x/d_i=6.4$



$\langle (\partial\phi_2/\partial x)^2 | \phi_1, \phi_2 \rangle$ at $x/d_i=20.1$



Conclusions & Future Work

- Developed 3-wire, thermal-anemometry-based probe capable of simultaneously measuring 2 scalars *and* velocity in a turbulent flow
- Made measurements of velocity and 2 scalars in a coaxial jet with a co-flow
- Future work will involve:
 - Pursuing additional noise reduction techniques
 - Furthering the understanding both the physics and modelling of multi-scalar mixing by way of simultaneous U, C & T measurements

Questions?